

CS667/CO681/PH767 Potential Project Topics

Note: You should feel free to pursue a project not on this list

Quantum walks: These can be used as quantum analogues of random walks, and have been shown to be useful for algorithmic purposes.

Two survey papers:

J. Kempe, “Quantum random walks – an introductory overview”.

<http://arxiv.org/abs/quant-ph/0303081>

A. Ambainis, “Quantum walks and their algorithmic applications”.

<http://arxiv.org/abs/quant-ph/0403120>

Also, a paper by:

F. Magniez, A. Nayak, J. Roland, and M. Santha, “Search via Quantum Walk”.

<http://arxiv.org/abs/quant-ph/0608026>

Here are a few more papers in this area. Part of the second reference and the third reference concern a *continuous-time* quantum walk.

H. Krovi, F. Magniez, M. Ozols, and J. Roland, “Finding is as easy as detecting for quantum walks”. <http://arxiv.org/abs/1002.2419>

C. Moore and A. Russell, “Quantum Walks on the Hypercube”.

<http://arxiv.org/abs/quant-ph/0104137>

A. M. Childs, “Universal computation by quantum walk”.

<http://arxiv.org/abs/0806.1972>

Quantum algorithms for solvable groups: Interesting algorithm for computing the size of solvable groups, and testing membership in such a group.

J. Watrous, “Quantum algorithms for solvable groups”.

<http://arxiv.org/abs/quant-ph/0011023>

Developments in quantum algorithms for evaluating AND-OR trees: These can be viewed as trees—such as balanced binary trees—whose gates at each level alternate between AND and OR gates, and whose leaves are labelled x_1, \dots, x_n . The goal is to evaluate the root of the tree with as few queries to the input values as possible. Classically, the cost has been long known to be $O(n^{0.753\dots})$, by an “alpha-beta pruning” technique. It has recently been shown that quantum algorithms can do better than this: $O(n^{0.5})$, for balanced binary trees (and this performance is also known to be optimal). This quantum algorithm has implications for game trees (for example, for more efficient algorithms for Chess and Go).

The development can be traced by the sequence of papers below. The first one is written in a physicist's language, and the subsequent ones are from a more "computer science" perspective. Nevertheless, this may be a challenging topic to digest in the context of a course project—the recommended approach is to focus technically on one aspect of the subject, while giving a non-technical broad overview to put things in context.

E. Farhi, J. Goldstone, S. Gutmann, "A Quantum Algorithm for the Hamiltonian NAND Tree".

<http://arxiv.org/abs/quant-ph/0702144>

A. Childs, B. Reichardt, R. Spalek, S. Zhang, "Every NAND formula of size N can be evaluated in time $N^{1/2+o(1)}$ on a quantum computer".

<http://arxiv.org/abs/quant-ph/0703015>

A. Ambainis, "A nearly optimal discrete query quantum algorithm for evaluating NAND formulas".

<http://arxiv.org/abs/0704.3628>

B. Reichardt, R. Spalek, "Span-program-based quantum algorithm for evaluating formulas".

<http://arxiv.org/abs/0710.2630>

The theory of fault-tolerant computing: These (lengthy) papers show that arbitrarily large quantum computers can be built from finite components whose accuracy and resilience to noise is bounded below some fixed constant. An overview and detailed explanation of some key component of one of these papers would be suitable for a course project.

D. Aharonov and M. Ben-Or, "Fault-Tolerant Quantum Computation with Constant Error Rate". <http://arxiv.org/abs/quant-ph/9906129>

J. Preskill, "Fault-tolerant quantum computation".

<http://arxiv.org/abs/quant-ph/9712048>

E. Knill, R. Laflamme, W. Zurek, "Threshold Accuracy for Quantum Computation". <http://arxiv.org/abs/quant-ph/9610011>

Quantum "proof systems": A number of results have emerged showing that the expressive power of proof systems increases when quantum information is available.

J. Watrous, “Succinct quantum proofs for properties of finite groups”.
<http://arxiv.org/abs/cs.CC/0009002>

J. Watrous, “PSPACE has 2-round quantum interactive proof systems”.
<http://arxiv.org/abs/cs.CC/9901015>

Continuous-time quantum algorithms: This is a variant of the query (black-box) model where queries can occur continuously in time.

E. Farhi and S. Gutman, “An Analog Analogue of a Digital Quantum Computation”. <http://arxiv.org/abs/quant-ph/9612026>

C. Mochon, “Hamiltonian Oracles”. <http://arxiv.org/abs/quant-ph/0602032>

Quantum self-testing: This is about verifying quantum devices that may be provided by adversarial parties.

F. Magniez, D. Mayers, M. Mosca, H. Ollivier, “Self-Testing of Quantum Circuits”. <http://arxiv.org/abs/quant-ph/0512111>

Classical simulations of stabilizer circuits: This is about an interesting restricted class of quantum circuits that is useful for quantum error-correction, but nevertheless can be efficiently simulated classically.

S. Aaronson and D. Gottesman, “Improved Simulation of Stabilizer Circuits”.
<http://arxiv.org/abs/quant-ph/0406196>

The hidden subgroup problem, as well as the *hidden shift problem*: Simon’s Algorithm, as well as Shor’s Algorithms for factoring and discrete log can be seen as solving a more abstract problem: the *hidden subgroup problem*. See also survey (1) for a broad overview.

This paper shows that the general case can be solved very efficiently in terms of black-box queries, but it uses exponentially many auxiliary operations:

M. Ettinger, P. Høyer, E. Knill, “The quantum query complexity of the hidden subgroup problem is polynomial”. <http://arxiv.org/abs/quant-ph/0401083>

This paper considers the hidden subgroup problem for a particular non-abelian group:

G. Kuperberg, “A subexponential-time quantum algorithm for the dihedral hidden subgroup problem”. <http://arxiv.org/abs/quant-ph/0302112>

Other papers related to the hidden subgroup problem:

O. Regev, “A Subexponential Time Algorithm for the Dihedral Hidden Subgroup Problem with Polynomial Space”. <http://arxiv.org/abs/quant-ph/0406151>

G. Ivanyos, L. Sanselme, M. Santha, “An efficient quantum algorithm for the hidden subgroup problem in nil-2 groups”. <http://arxiv.org/abs/0707.1260>

G. Ivanyos, L. Sanselme, M. Santha, “An efficient quantum algorithm for the hidden subgroup problem in extraspecial groups”.
<http://arxiv.org/abs/quant-ph/0701235>

Van Dam, S. Hallgren, and L. Ip, “Quantum Algorithms for some Hidden Shift Problems”. <http://arxiv.org/abs/quant-ph/0211140>

A. Childs and W. van Dam, “Quantum algorithm for a generalized hidden shift problem”. <http://arxiv.org/abs/quant-ph/0507190>

Quantum Shannon theory: A generalization of classical Shannon theory, concerned with the capacities of noisy channels (quantum and classical). See also surveys (2) and (3) at the end of this document for a broad overview. The third reference makes an interesting connection with the so-called “black hole information” paradox.

P. Shor, “Capacities of quantum channels: how to find them”.
<http://xxx.lanl.gov/abs/quant-ph/0304102>

C. H. Bennett, I. Devetak, A. W. Harrow, P. W. Shor, A. Winter, “Quantum Reverse Shannon Theorem”. <http://arxiv.org/abs/0912.5537>

T. S. Cubitt, D. Leung, W. Matthews, A. Winter, “Improving zero-error classical communication with entanglement”. <http://arxiv.org/abs/0911.5300>

P. Hayden and J. Preskill “Black holes as mirrors: quantum information in random subsystems”. <http://arxiv.org/abs/0708.4025>

M. Horodecki, J. Oppenheim, A. Winter “Quantum information can be negative”.
<http://arxiv.org/abs/quant-ph/0505062>

G. Smith, J. Yard, “Quantum Communication With Zero-Capacity Channels”.
<http://arxiv.org/abs/0807.4935>

Quantum algorithms for miscellaneous “traditional” problems: Employs quantum algorithms to obtain speed-ups for various traditional problems in computer science.

A. Ambainis and R. Spalek, “Quantum algorithms for matching and network flows”. <http://arxiv.org/abs/quant-ph/0508205>

C. Durr, M. Heiligman, P. Høyer, M. Mhalla “Quantum query complexity of some graph problems”. <http://arxiv.org/abs/quant-ph/0401091>

B. Furrow, “A panoply of quantum algorithms”.
<http://arxiv.org/abs/quant-ph/0606127>

Oracle interrogation: Addresses the problem of *completely* determining a function $f: \{0,1\}^n \rightarrow \{0,1\}$.

W. van Dam, “Quantum oracle interrogation: getting all information for almost half the price”. <http://arxiv.org/abs/quant-ph/9805006>

Linear optics: Proposes problems that are “hard” in a complexity theoretic sense but nevertheless solvable by easily implementable quantum computers. (Warning: the definitions of the problems and their hardness are somewhat subtle.)

S. Aaronson, A. Arkhipov, “The Computational Complexity of Linear Optics”.
<http://arxiv.org/abs/1011.3245>

Approximating any unitary gate from a simple set of generating operations:

Y. Shi, “Both Toffoli and Controlled-NOT need little help to do universal quantum computation”. <http://arxiv.org/abs/quant-ph/0205115>

Quantum computation using only measurement gates:

R. Jozsa, “An introduction to measurement based quantum computation”.
<http://arxiv.org/abs/quant-ph/0508124>

Using the mathematics of quantum information to prove theorems: There are a few mathematical theorems whose statements seem to have nothing to do with quantum information, but which have been reduced to questions about quantum information and then proved by techniques of quantum information. These are applications of quantum computing that stand whether or not one ever builds a quantum computer! (Note: this is quite different from the topic “Quantum ‘proof systems’,” which is also interesting but for different reasons.)

A good survey:

A. Drucker, R. de Wolf, “Quantum Proofs for Classical Theorems”.
<http://arxiv.org/abs/0910.3376>

A recent breakthrough, where quantum computing ideas were used to resolve a 20-year-old problem, by proving that linear programs (used in a certain way) cannot be used to solve NP-complete problems:

S. Fiorini, S. Massar, S. Pokutta, H. R. Tiwary, R. de Wolf, Linear vs. “Semidefinite Extended Formulations: Exponential Separation and Strong Lower Bounds” <http://arxiv.org/abs/1111.0837>

A nice quantum proof of a classical result in computational complexity about the hardness of computing the permanent:

S. Aaronson, “A Linear-Optical Proof that the Permanent is #P-Hard” <http://arxiv.org/abs/1109.1674>

Complexity of finding the minimum eigenvalue of certain Hamiltonians: Related to the “minimum energy levels” of a certain quantum mechanical systems

J. Kempe, A. Kitaev, O. Regev, “The Complexity of the Local Hamiltonian Problem”. <http://arxiv.org/abs/quant-ph/0406180>

Quantum money: The idea is for people to circulate quantum states around that have properties that cash has (or should have): it cannot be counterfeited, its validity can be checked without having to interact with bank (unlike debit cards), it is anonymous (it cannot be traced back to a spender. With classical information, this is information theoretically impossible, even under cryptographic assumptions about (say) trapdoor or one-way functions. With quantum information and computational assumptions, it is conceivable that this can be done. The following paper is a recent one that is advanced but very well written. A component of this paper could be the basis of a project topic. For example, “mini-schemes”.

Scott Aaronson, Paul Christiano, “Quantum Money from Hidden Subspaces” <http://arxiv.org/abs/1203.4740>

Using “nonlocal” behaviour to accomplish various things securely: What can you do securely even if you are using devices supplied by your adversary? Although this may look like a hopeless situation, one can actually use properties of quantum information (in nonlocal settings) to “guarantee” certain things, such as: bit strings actually being certifiable random, cryptographic keys being secure, and more.

U.V. Vazirani and T. Vidick, “Certifiable Quantum Dice - Or, testable exponential randomness expansion” <http://arxiv.org/abs/1111.6054>

U.V. Vazirani and T. Vidick, “Fully device independent quantum key distribution” <http://arxiv.org/abs/1210.1810>

B.W. Reichardt, F. Unger, U. Vazirani, “Classical command of quantum systems via rigidity of CHSH games” <http://arxiv.org/abs/1209.0449>

Quantum Algorithms for Quantum Field Theories: Using a quantum computer to simulate problems in quantum field theory (where quantum mechanical as well relativistic effects occur). It’s probably good to be already familiar with quantum field theory to tackle this one:

S. P. Jordan, K. S. M. Lee, J. Preskill, “Quantum Algorithms for Quantum Field Theories”, <http://arxiv.org/abs/1111.3633>

Blind quantum computing: Suppose that you want to compute something on someone else’s quantum computer without revealing any information about what you are computing. This paper addresses this issue:

A. Broadbent, J. Fitzsimons, E. Kashefi, “Universal blind quantum computation” <http://arxiv.org/abs/0807.4154>

Merkle puzzles: A nice toy problem related to cryptography in a quantum world:

G. Brassard, P. Hoyer, K. Kalach, M. Kaplan, S. Laplante, L. Salvail, “Merkle Puzzles in a Quantum World” <http://arxiv.org/abs/1108.2316>

Surveys:

These are included for you to peruse for a broad perspective about an “area of research”. You might select a topic based on a specific part of one of these surveys (the entire survey would be long). In some cases, this list (above) or the originally posted list already has an item pertaining to a section of the survey.

- (1) A. Childs and W. van Dam, “Quantum algorithms for algebraic problems”.
<http://arxiv.org/abs/0812.0380>
- (2) I. Devetak, A.W. Harrow, and A. Winter, “A resource framework for quantum algorithms”.<http://arxiv.org/abs/quant-ph/0512015>
- (3) G. Smith, “Quantum Channel Capacities”.
<http://arxiv.org/abs/1007.2855>
- (4) J. Watrous, “Quantum Computational Complexity”.
<http://arxiv.org/abs/0804.3401>

Boson Sampling is computationally hard for classical computers but accomplished by quantum computers:

S. Aaronson, A. Arkhipov, “The Computational Complexity of Linear Optics”
<http://arxiv.org/abs/1011.3245>

An interesting connection between state transformation problems and the exponent for matrix multiplication:

P. Vrana, M. Christandl, “Asymptotic entanglement transformation between W and GHZ states” <http://arxiv.org/abs/1310.3244>

Quantum information results pertaining to the issue of information escaping from black holes:

P. Hayden, J. Preskill, “Black holes as mirrors: quantum information in random subsystems” <http://arxiv.org/abs/0708.4025>

D. Harlow and P. Hayden, “Quantum Computation vs. Firewalls” <http://arxiv.org/abs/1301.4504>